

Supporting Information

Optimization of the interatomic distance in the [Gd-O]⁺ cation

In order to ensure ourselves that the obtained short bond length in Dy-O⁺ (Figure 1) is not accidental, we performed the geometry optimization of a similar complex Gd-O⁺, and check the result against the size of the used active spaces of the multiconfigurational self-consistent field method (CASSCF) and additional account of dynamical correlation (CASPT2).

Optimization of the distance in the Gd-O⁺ cation was performed with MOLCAS at the CASSCF/CASPT2 level of theory, using the Triple-Zeta Polarized (TZP) basis sets for both atoms from ANO-RCC Basis Set Library available in MOLCAS. The following contractions were employed:

Gd – ANO-RCC...8s7p5d4f2g1h.

O – ANO-RCC...4s3p2d1f.

Three active spaces were considered for the CASSCF method:

AS1 — restricted active space – 7 electrons in 7 orbitals (the 4f shell of the Gd) — CAS(7 in 7).

AS2 — Gd(4f shell) + O{2px,2py,2pz}+3 virtual orbitals — CAS(13 in 13).

AS3 — Gd(4f shell) + O{2s,2px,2py,2pz}+4 virtual orbitals — CAS(15 in 15).

Dynamic correlation was added by means of the CASPT2 program.

| | Level of theory | Active space | R (in Å) | Charge on Gd | Charge on O | Natural Bond Order* |
|---|-----------------|--------------|----------|--------------|-------------|---------------------|
| 1 | CASSCF | AS1 | 1.75 | 1.7454 | -0.7454 | 4.985 |
| 2 | CASSCF/CASPT2 | AS1 | 1.76 | 1.6907 | -0.6907 | 5.987 |
| 3 | CASSCF | AS2 | 1.79 | 1.5910 | -0.5910 | 1.983 |
| 4 | CASSCF/CASPT2 | AS2 | 1.76 | 1.5510 | -0.5510 | 3.971 |
| 5 | CASSCF | AS3 | 1.78 | 1.5983 | -0.5983 | 5.844 |
| 6 | CASSCF/CASPT2 | AS3 | 1.75 | 1.5411 | -0.5411 | 5.817 |

* -- obtained from the CASSCF program.

For the cation [Dy-O]⁺ a slightly smaller bond length is expected (Figure 1) because of a smaller radius of Dy³⁺ compared to Gd³⁺.

Computational details:

The entire Dy₃ triangle was computed ab initio: no optimization of the structure was done.

In order to compute the energy spectrum of the individual Dy centers, the neighboring Dy ions were computationally simulated by a diamagnetic closed-shell La³⁺.

Active space of the Complete Active Space Self-Consistent field method included the 4f shell of the Dy³⁺ ion: CAS(9 in 7).

Spin-orbit coupling was done by the Restricted Active Space State Interaction (RASSI) method. The number of states included in the spin-orbit coupling (RASSI) was 21 sextets (all) 108 quartets (224 in total) and 32 doublets (490 in total). Including more states would probably change the states which are very high in energy, while the energies and magnetic properties of the lowest states remain the same.

All basis sets were taken from the ANO-RCC basis set library available in MOLCAS. The following contractions were used:

Dy, La -- 7s6p4d3f1g.

Cl -- 4s3p.

O, N, C -- 3s2p.

H.-- 2s.

This afforded a set of 664 basis functions which were further used in the CASSCF/RASSI programs.

Table S1: CASSCF (spin-free) and RASSI (spin-orbit) energies (cm⁻¹) for Dy1-Dy3 centers in Dy₃ triangle.

| Spin Multiplicity | CASSCF | | | RASSI | | |
|----------------------|-------------|-----------|----------|----------|----------|----------|
| | 1 | 2 | 3 | 1 | 2 | 3 |
| 6 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| | 6.914 | 2.091 | 34.429 | 223.555 | 130.353 | 103.476 |
| | 310.476 | 197.261 | 100.608 | 357.842 | 273.744 | 141.038 |
| | 380.549 | 217.861 | 177.968 | 443.316 | 390.084 | 171.100 |
| | 485.781 | 413.776 | 219.825 | 506.003 | 464.282 | 208.691 |
| | 6H 498.163 | 468.672 | 266.042 | 541.690 | 513.565 | 228.586 |
| | 555.171 | 525.403 | 283.091 | 582.487 | 577.534 | 287.051 |
| | 619.799 | 589.381 | 332.093 | 622.393 | 699.696 | 395.074 |
| | 626.464 | 605.677 | 334.203 | 3631.505 | 3575.763 | 3566.062 |
| | 664.782 | 743.297 | 469.169 | 3767.427 | 3728.404 | 3628.893 |
| | 673.407 | 750.799 | 485.901 | 3880.100 | 3825.851 | 3667.381 |
| | 7748.439 | 7716.354 | 7569.958 | 3951.925 | 3902.917 | 3689.112 |
| | 7772.399 | 7740.964 | 7634.101 | 3992.281 | 3968.580 | 3721.390 |
| | 7864.434 | 7854.917 | 7660.064 | 4033.476 | 4027.186 | 3754.292 |
| | 6F 7933.689 | 7901.437 | 7721.728 | 4079.714 | 4113.021 | 3797.647 |
| | 7959.947 | 7921.467 | 7746.345 | 6245.970 | 6172.193 | 6129.318 |
| | 7989.872 | 7977.258 | 7781.261 | 6328.442 | 6306.240 | 6175.260 |
| | 8001.254 | 7995.910 | 7783.440 | 6410.074 | 6383.502 | 6201.756 |
| 6P 34785.778 | 34722.573 | 34849.737 | 6479.141 | 6440.971 | 6219.078 | |
| 35292.229 | 35267.587 | 34987.968 | 6526.664 | 6513.050 | 6267.326 | |

| | | | | | | |
|-----|-----------|-----------|-----------|-----------|-----------|-----------|
| | 35495.540 | 35535.525 | 35168.419 | 6612.469 | 6620.108 | 6318.432 |
| 4 | 24969.288 | 24960.051 | 24886.147 | 8236.342 | 8166.178 | 8085.637 |
| | 24973.403 | 24963.039 | 24894.519 | 8296.722 | 8288.602 | 8125.956 |
| | 25124.651 | 25065.113 | 24959.322 | 8386.182 | 8349.757 | 8156.256 |
| | 25133.550 | 25067.648 | 24967.050 | 8443.696 | 8421.077 | 8198.904 |
| | 25202.574 | 25140.083 | 24975.852 | 8543.882 | 8544.870 | 8263.910 |
| | 25211.226 | 25157.396 | 24977.316 | 9779.193 | 9716.942 | 9611.188 |
| | 25221.475 | 25178.115 | 24984.643 | 9860.103 | 9847.666 | 9676.577 |
| | 25236.700 | 25215.366 | 25013.649 | 9961.883 | 9927.103 | 9723.917 |
| | 25248.175 | 25238.706 | 25024.665 | 10061.544 | 10064.545 | 9784.673 |
| | 25260.750 | 25249.512 | 25058.927 | 10146.624 | 10119.223 | 9967.826 |
| | 25278.689 | 25273.308 | 25066.958 | 10211.087 | 10178.168 | 10009.150 |
| | 25308.500 | 25278.310 | 25105.642 | 10249.551 | 10218.951 | 10025.167 |
| | 25320.212 | 25291.745 | 25118.389 | 10272.599 | 10259.982 | 10061.698 |
| | 25386.639 | 25361.738 | 25212.631 | 10331.645 | 10299.857 | 10073.209 |
| | 25396.893 | 25405.608 | 25235.076 | 10343.643 | 10342.830 | 10103.747 |
| | 25413.836 | 25411.184 | 25248.800 | 10938.349 | 10882.896 | 10803.037 |
| | 25432.651 | 25428.549 | 25280.983 | 11185.953 | 11140.801 | 10911.163 |
| | 25442.530 | 25434.897 | 25295.715 | 11263.296 | 11292.775 | 10992.428 |
| | 25457.743 | 25440.680 | 25304.905 | 11741.275 | 11702.593 | 11518.547 |
| | 25465.146 | 25451.914 | 25309.835 | 11750.240 | 11724.653 | 11543.097 |
| ... | ... | ... | 11757.030 | 11738.483 | 11550.133 | |
| 2 | 37513.109 | 37493.317 | 37337.482 | 11780.641 | 11775.471 | 11562.359 |
| | 37514.249 | 37494.871 | 37347.137 | 11836.501 | 11815.478 | 11588.881 |
| | 37559.787 | 37526.057 | 37363.862 | 13666.025 | 13642.379 | 13445.736 |
| | 37571.512 | 37532.184 | 37368.460 | 13675.400 | 13656.386 | 13460.655 |
| | 37577.972 | 37548.100 | 37380.434 | 13730.243 | 13703.776 | 13508.642 |
| | 37585.397 | 37576.799 | 37399.119 | 13754.708 | 13736.568 | 13525.798 |
| | 37597.500 | 37601.369 | 37413.278 | 15127.373 | 15111.572 | 14913.240 |
| | 37655.921 | 37612.800 | 37457.156 | 15162.077 | 15134.783 | 14938.245 |
| | 37677.228 | 37644.754 | 37475.092 | 15199.709 | 15178.376 | 14973.922 |
| | 37683.821 | 37683.477 | 37484.813 | 16057.699 | 16036.400 | 15836.563 |
| | 37710.886 | 37712.838 | 37547.491 | 16063.673 | 16042.509 | 15840.672 |
| | 37720.716 | 37718.719 | 37555.628 | 16530.233 | 16511.127 | 16305.118 |
| | 37756.930 | 37728.746 | 37556.944 | 25275.996 | 25231.763 | 25159.085 |
| | 37765.355 | 37729.987 | 37566.883 | 25357.352 | 25336.479 | 25187.021 |
| | 37768.643 | 37744.505 | 37587.548 | 25409.704 | 25380.788 | 25199.628 |
| | 37775.554 | 37766.615 | 37599.714 | 25464.686 | 25426.796 | 25242.674 |
| | 37787.437 | 37781.623 | 37603.563 | 25487.525 | 25463.087 | 25294.315 |
| | 39144.750 | 39142.990 | 39011.362 | 25554.200 | 25542.096 | 25332.405 |
| | 39145.247 | 39143.765 | 39014.485 | 25580.130 | 25566.312 | 25347.233 |
| | 39254.330 | 39213.066 | 39054.890 | 25609.162 | 25613.468 | 25380.689 |
| ... | ... | ... | ... | ... | ... | |

Table S2: Comparative g_x , g_y , g_z for 8 lowest Kramers doublets of the Dy1-Dy3 centers of the Dy₃ triangle.

| KD | 1 | | 2 | | 3 | | |
|----|-----------------------|---------|-----------------------|---------|-----------------------|---------|---------|
| | E (cm ⁻¹) | g | E (cm ⁻¹) | g | E (cm ⁻¹) | g | |
| 1 | g_x | | 0.0015 | | 0.0048 | | 0.0088 |
| | g_y | 0.000 | 0.0026 | 0.000 | 0.0072 | 0.000 | 0.0341 |
| | g_z | | 19.7285 | | 19.5877 | | 19.6673 |
| 2 | g_x | | 0.0302 | | 0.0263 | | 0.3985 |
| | g_y | 223.555 | 0.0430 | 130.353 | 0.0295 | 103.476 | 0.6451 |
| | g_z | | 16.6940 | | 16.7704 | | 17.7500 |
| 3 | g_x | | 0.9851 | | 0.1991 | | 3.4955 |
| | g_y | 357.842 | 1.1679 | 273.744 | 0.2423 | 141.038 | 3.6706 |
| | g_z | | 13.6251 | | 13.9970 | | 11.3661 |
| 4 | g_x | | 4.2030 | | 0.8390 | | 2.2148 |
| | g_y | 443.316 | 5.4340 | 390.084 | 1.0588 | 171.100 | 4.9693 |
| | g_z | | 8.9738 | | 11.0519 | | 11.7486 |
| 5 | g_x | | 2.2538 | | 3.7772 | | 0.0690 |
| | g_y | 506.003 | 3.0835 | 464.282 | 5.3005 | 208.691 | 3.2231 |
| | g_z | | 13.9778 | | 8.5234 | | 14.0985 |
| 6 | g_x | | 0.1392 | | 2.0094 | | 1.2158 |
| | g_y | 541.690 | 1.7831 | 513.565 | 3.6592 | 228.586 | 3.0479 |
| | g_z | | 13.6022 | | 14.2754 | | 16.4501 |
| 7 | g_x | | 0.2282 | | 0.2872 | | 0.1044 |
| | g_y | 582.487 | 0.6579 | 577.534 | 0.7102 | 287.051 | 0.2814 |
| | g_z | | 17.4705 | | 18.0290 | | 18.7437 |
| 8 | g_x | | 0.0738 | | 0.0182 | | 0.0022 |
| | g_y | 622.393 | 0.1792 | 699.696 | 0.0383 | 395.074 | 0.0087 |
| | g_z | | 18.8487 | | 19.5646 | | 19.5569 |

Table S3: *g*-factors and main magnetic axes (3×3) for 8 lowest Kramers doublets of the Dy1 center from Dy₃ triangle.

| KD | E (cm ⁻¹) | | <i>g</i> | <i>x</i> | <i>y</i> | <i>z</i> |
|----------|-----------------------|----------------------|----------|----------|----------|----------|
| 1 | 0.000 | <i>g_X</i> | 0.0015 | 0.9883 | 0.0310 | -0.1495 |
| | | <i>g_Y</i> | 0.0026 | -0.1527 | 0.1821 | -0.9714 |
| | | <i>g_Z</i> | 19.7285 | -0.0029 | 0.9828 | 0.1847 |
| 2 | 223.555 | <i>g_X</i> | 0.0302 | 0.9960 | 0.0313 | 0.0836 |
| | | <i>g_Y</i> | 0.0430 | 0.0824 | 0.0365 | -0.9959 |
| | | <i>g_Z</i> | 16.6940 | -0.0342 | 0.9988 | 0.0338 |
| 3 | 357.842 | <i>g_X</i> | 0.9851 | 0.9438 | 0.0367 | -0.3285 |
| | | <i>g_Y</i> | 1.1679 | 0.3146 | 0.2056 | 0.9267 |
| | | <i>g_Z</i> | 13.6251 | 0.1015 | -0.9780 | 0.1825 |
| 4 | 443.316 | <i>g_X</i> | 4.2030 | 0.3368 | 0.3735 | 0.8643 |
| | | <i>g_Y</i> | 5.4340 | -0.9345 | 0.0202 | 0.3555 |
| | | <i>g_Z</i> | 8.9738 | 0.1153 | -0.9274 | 0.3558 |
| 5 | 506.003 | <i>g_X</i> | 2.2538 | -0.6853 | -0.3473 | 0.6402 |
| | | <i>g_Y</i> | 3.0835 | 0.1742 | -0.9316 | -0.3189 |
| | | <i>g_Z</i> | 13.9778 | 0.7071 | -0.1070 | 0.6989 |
| 6 | 541.690 | <i>g_X</i> | 0.1392 | -0.2467 | -0.9453 | -0.2134 |
| | | <i>g_Y</i> | 1.7831 | 0.8441 | -0.3177 | 0.4318 |
| | | <i>g_Z</i> | 13.6022 | -0.4760 | -0.0736 | 0.8764 |
| 7 | 582.487 | <i>g_X</i> | 0.2282 | 0.3345 | -0.9199 | -0.2049 |
| | | <i>g_Y</i> | 0.6579 | 0.4096 | -0.0539 | 0.9107 |
| | | <i>g_Z</i> | 17.4705 | -0.8487 | -0.3885 | 0.3587 |
| 8 | 622.393 | <i>g_X</i> | 0.0738 | 0.1884 | 0.9613 | -0.2013 |
| | | <i>g_Y</i> | 0.1792 | -0.4824 | -0.0879 | -0.8715 |
| | | <i>g_Z</i> | 18.8487 | -0.8554 | 0.2613 | 0.4472 |

Table S4: Relative angles between the main anisotropy axes in different doublet states of the Dy1 center from Dy₃ triangle.

| KD | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0.00 | 8.41 | 20.62 | 29.66 | 89.27 | 86.44 | 74.24 | 71.62 |
| 2 | 8.41 | 0.00 | 12.20 | 21.23 | 82.28 | 87.98 | 71.67 | 73.64 |
| 3 | 20.62 | 12.20 | 0.00 | 9.21 | 71.65 | 80.90 | 69.78 | 76.02 |
| 4 | 29.66 | 21.23 | 9.21 | 0.00 | 65.27 | 73.97 | 66.67 | 80.39 |
| 5 | 89.27 | 82.28 | 71.65 | 65.27 | 0.00 | 82.75 | 75.80 | 69.44 |
| 6 | 86.44 | 87.98 | 80.90 | 73.97 | 82.75 | 0.00 | 29.31 | 31.81 |
| 7 | 74.24 | 71.67 | 69.78 | 66.67 | 75.80 | 29.31 | 0.00 | 34.73 |
| 8 | 71.62 | 73.64 | 76.02 | 80.39 | 69.44 | 31.81 | 34.73 | 0.00 |

Table S5: *g*-factors and main magnetic axes (3×3) for 8 lowest Kramers doublets of the Dy₂ center from Dy₃ triangle.

| KD | E (cm ⁻¹) | | <i>g</i> | <i>x</i> | <i>y</i> | <i>z</i> |
|----------|-----------------------|----------------------|----------|----------|----------|----------|
| 1 | 0.000 | <i>g_X</i> | 0.0048 | -0.8920 | -0.1358 | 0.4312 |
| | | <i>g_Y</i> | 0.0072 | 0.3713 | -0.7642 | 0.5273 |
| | | <i>g_Z</i> | 19.5877 | 0.2579 | 0.6305 | 0.7321 |
| 2 | 130.353 | <i>g_X</i> | 0.0263 | 0.9624 | -0.2687 | 0.0389 |
| | | <i>g_Y</i> | 0.0295 | 0.2165 | 0.6731 | -0.7072 |
| | | <i>g_Z</i> | 16.7704 | 0.1638 | 0.6890 | 0.7060 |
| 3 | 273.744 | <i>g_X</i> | 0.1991 | -0.8093 | -0.3135 | 0.4967 |
| | | <i>g_Y</i> | 0.2423 | 0.5745 | -0.5987 | 0.5582 |
| | | <i>g_Z</i> | 13.9970 | 0.1224 | 0.7371 | 0.6646 |
| 4 | 390.084 | <i>g_X</i> | 0.8390 | -0.4714 | 0.5332 | -0.7025 |
| | | <i>g_Y</i> | 1.0588 | -0.8806 | -0.2414 | 0.4078 |
| | | <i>g_Z</i> | 11.0519 | 0.0478 | 0.8108 | 0.5833 |
| 5 | 464.282 | <i>g_X</i> | 3.7772 | -0.8255 | -0.2033 | -0.5266 |
| | | <i>g_Y</i> | 5.3005 | -0.4727 | -0.2608 | 0.8417 |
| | | <i>g_Z</i> | 8.5234 | -0.3084 | 0.9437 | 0.1192 |
| 6 | 513.565 | <i>g_X</i> | 2.0094 | 0.4670 | 0.5980 | 0.6514 |
| | | <i>g_Y</i> | 3.6592 | -0.8837 | 0.3424 | 0.3191 |
| | | <i>g_Z</i> | 14.2754 | -0.0322 | -0.7246 | 0.6884 |
| 7 | 577.534 | <i>g_X</i> | 0.2872 | 0.4596 | 0.5503 | 0.6971 |
| | | <i>g_Y</i> | 0.7102 | -0.5348 | 0.7981 | -0.2774 |
| | | <i>g_Z</i> | 18.0290 | -0.7090 | -0.2454 | 0.6611 |
| 8 | 699.696 | <i>g_X</i> | 0.0182 | 0.1244 | -0.8781 | -0.4620 |
| | | <i>g_Y</i> | 0.0383 | 0.0276 | 0.4685 | -0.8830 |
| | | <i>g_Z</i> | 19.5646 | 0.9919 | 0.0971 | 0.0825 |

Table S6: Relative angles between the main anisotropy axes in different doublet states of the Dy₂ center from Dy₃ triangle.

| KD | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0.00 | 5.66 | 9.30 | 15.97 | 45.09 | 88.68 | 82.86 | 69.30 |
| 2 | 5.66 | 0.00 | 4.00 | 10.89 | 40.13 | 88.98 | 80.35 | 74.33 |
| 3 | 9.30 | 4.00 | 0.00 | 6.96 | 36.17 | 85.75 | 80.66 | 76.52 |
| 4 | 15.97 | 10.89 | 6.96 | 0.00 | 29.26 | 79.96 | 81.60 | 80.21 |
| 5 | 45.09 | 40.13 | 36.17 | 29.26 | 0.00 | 57.40 | 85.22 | 82.29 |
| 6 | 88.68 | 88.98 | 85.75 | 79.96 | 57.40 | 0.00 | 51.41 | 87.67 |
| 7 | 82.86 | 80.35 | 80.66 | 81.60 | 85.22 | 51.41 | 0.00 | 44.83 |
| 8 | 69.30 | 74.33 | 76.52 | 80.21 | 82.29 | 87.67 | 44.83 | 0.00 |

Table S7: *g*-factors and main magnetic axes (3×3) for 8 lowest Kramers doublets of the Dy₃ center from Dy₃ triangle.

| KD | E (cm ⁻¹) | | <i>g</i> | <i>x</i> | <i>y</i> | <i>z</i> |
|----------|-----------------------|----------------------|----------|----------|----------|----------|
| 1 | 0.000 | <i>g_X</i> | 0.0088 | 0.9358 | 0.3501 | -0.0414 |
| | | <i>g_Y</i> | 0.0341 | -0.2162 | 0.6628 | 0.7169 |
| | | <i>g_Z</i> | 19.6673 | 0.2784 | -0.6619 | 0.6959 |
| 2 | 103.476 | <i>g_X</i> | 0.3985 | 0.8841 | 0.3838 | -0.2665 |
| | | <i>g_Y</i> | 0.6451 | -0.3729 | 0.9233 | 0.0925 |
| | | <i>g_Z</i> | 17.7500 | 0.2815 | 0.0176 | 0.9594 |
| 3 | 141.038 | <i>g_X</i> | 3.4955 | 0.1532 | 0.9880 | 0.0202 |
| | | <i>g_Y</i> | 3.6706 | -0.8300 | 0.1176 | 0.5452 |
| | | <i>g_Z</i> | 11.3661 | 0.5363 | -0.1003 | 0.8381 |
| 4 | 171.100 | <i>g_X</i> | 2.2148 | 0.0546 | 0.0617 | 0.9966 |
| | | <i>g_Y</i> | 4.9693 | 0.4811 | -0.8729 | 0.0804 |
| | | <i>g_Z</i> | 11.7486 | 0.8749 | 0.4839 | 0.0180 |
| 5 | 208.691 | <i>g_X</i> | 0.0690 | 0.5153 | 0.6266 | -0.5847 |
| | | <i>g_Y</i> | 3.2231 | -0.8373 | 0.2226 | -0.4994 |
| | | <i>g_Z</i> | 14.0985 | -0.1828 | 0.7469 | 0.6393 |
| 6 | 228.586 | <i>g_X</i> | 1.2158 | -0.5445 | 0.4187 | -0.7268 |
| | | <i>g_Y</i> | 3.0479 | -0.7972 | 0.0111 | 0.6036 |
| | | <i>g_Z</i> | 16.4501 | 0.2608 | 0.9081 | 0.3278 |
| 7 | 287.051 | <i>g_X</i> | 0.1044 | -0.1898 | -0.1922 | 0.9628 |
| | | <i>g_Y</i> | 0.2814 | -0.2326 | -0.9439 | -0.2343 |
| | | <i>g_Z</i> | 18.7437 | 0.9539 | -0.2684 | 0.1344 |
| 8 | 395.074 | <i>g_X</i> | 0.0022 | 0.6627 | -0.7400 | 0.1151 |
| | | <i>g_Y</i> | 0.0087 | 0.3303 | 0.4267 | 0.8419 |
| | | <i>g_Z</i> | 19.5569 | -0.6721 | -0.5199 | 0.5272 |

Table S8: Relative angles between the main anisotropy axes in different doublet states of the Dy₃ center from Dy₃ triangle.

| KD | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|----------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1 | 0.00 | 43.65 | 37.03 | 83.52 | 84.42 | 72.93 | 57.41 | 58.39 |
| 2 | 43.65 | 0.00 | 18.47 | 74.90 | 53.72 | 64.68 | 67.11 | 72.37 |
| 3 | 37.03 | 18.47 | 0.00 | 65.77 | 68.54 | 70.92 | 48.81 | 82.57 |
| 4 | 83.52 | 74.90 | 65.77 | 0.00 | 75.01 | 46.19 | 48.38 | 32.74 |
| 5 | 84.42 | 53.72 | 68.54 | 75.01 | 0.00 | 31.01 | 73.95 | 86.19 |
| 6 | 72.93 | 64.68 | 70.92 | 46.19 | 31.01 | 0.00 | 87.94 | 63.12 |
| 7 | 57.41 | 67.11 | 48.81 | 48.38 | 73.95 | 87.94 | 0.00 | 64.59 |
| 8 | 58.39 | 72.37 | 82.57 | 32.74 | 86.19 | 63.12 | 64.59 | 0.00 |

Table S9: CASSCF (spin-free) and RASSI (spin-orbit) energies (cm⁻¹) for Tb1-Tb3 centers in Tb₃ molecule.

| Spin Multiplicity | CASSCF | | | RASSI | | |
|-------------------|---------|---------|----------|----------|----------|----------|
| | 1 | 2 | 3 | 1 | 2 | 3 |
| 7 | 0.0 | 0.0 | 0.0 | 0.000 | 0.000 | 0.000 |
| | 92.0 | 38.8 | 157.6 | 0.131 | 0.029 | 0.090 |
| | 103.5 | 195.8 | 188.2 | 22.579 | 142.214 | 106.225 |
| | 162.5 | 345.2 | 282.1 | 26.390 | 144.587 | 107.496 |
| | 310.1 | 526.8 | 495.2 | 59.529 | 235.247 | 171.446 |
| | 578.3 | 677.1 | 631.0 | 80.723 | 242.520 | 178.386 |
| | 674.6 | 819.9 | 685.3 | 100.832 | 292.435 | 214.780 |
| | 25644.3 | 25699.8 | 25706.9 | 148.959 | 330.380 | 235.191 |
| 5 | 25646.3 | 25709.9 | 25717.0 | 154.370 | 356.951 | 242.988 |
| | 25723.0 | 25818.2 | 25798.4 | 275.726 | 390.849 | 275.819 |
| | 25739.4 | 25876.2 | 25854.7 | 279.138 | 402.843 | 277.512 |
| | 25753.8 | 25905.0 | 25868.1 | 347.074 | 623.244 | 485.772 |
| | 29132.8 | 29238.4 | 29263.5 | 348.359 | 623.458 | 485.818 |
| | 29141.1 | 29243.1 | 29263.7 | 2095.135 | 2227.202 | 2153.189 |
| | 29164.6 | 29258.4 | 29314.4 | 2097.977 | 2232.951 | 2175.865 |
| | 29172.8 | 29264.8 | 29315.6 | 2127.122 | 2259.951 | 2194.253 |
| | 29236.3 | 29337.7 | 29356.9 | 2150.358 | 2288.122 | 2219.502 |
| | ... | ... | ... | 2193.445 | 2326.271 | 2249.338 |
| | 3 | 47102.5 | 47199.8 | 47192.0 | 2258.577 | 2384.119 |
| 47104.6 | | 47205.8 | 47198.8 | 2288.914 | 2397.278 | 2312.073 |
| 47112.1 | | 47219.5 | 47208.2 | 2297.216 | 2473.503 | 2387.739 |
| 48215.5 | | 48304.1 | 48269.4 | 2302.357 | 2486.533 | 2392.897 |
| 48216.6 | | 48305.1 | 48269.5 | 2348.493 | 2540.629 | 2439.139 |
| 48231.2 | | 48328.0 | 48295.2 | 2365.063 | 2554.125 | 2442.956 |
| 48239.1 | | 48328.8 | 48295.6 | 3446.275 | 3577.850 | 3478.595 |
| 48252.9 | | 48344.5 | 48349.7 | 3452.561 | 3636.194 | 3566.922 |
| 48275.2 | | 48345.6 | 48352.0 | 3517.782 | 3648.473 | 3603.186 |
| 48279.8 | | 48374.2 | 48365.6 | 3534.211 | 3688.533 | 3650.930 |
| ... | | ... | ... | 3565.813 | 3717.299 | 3655.089 |
| 1 | 56773.3 | 56875.8 | 56871.4 | 3593.375 | 3780.941 | 3686.517 |
| | 57535.1 | 57590.5 | 57612.5 | 3683.947 | 3809.001 | 3715.080 |
| | 57536.5 | 57590.7 | 57613.0 | 3701.164 | 3840.996 | 3756.333 |
| | 57554.2 | 57638.3 | 57637.7 | 3722.555 | 3894.382 | 3774.043 |
| | 57555.4 | 57638.3 | 57638.8 | 4539.100 | 4676.831 | 4624.012 |
| | 57588.5 | 57683.2 | 57687.1 | 4561.129 | 4700.755 | 4644.695 |
| | 57592.5 | 57684.3 | 57687.8 | 4574.003 | 4720.701 | 4654.673 |
| | 57602.6 | 57713.9 | 57716.3 | 4622.909 | 4739.823 | 4686.317 |
| | 57624.1 | 57714.6 | 57718.5 | 4643.222 | 4814.801 | 4717.431 |
| | 57637.1 | 57763.0 | 57747.1 | 4662.720 | 4835.722 | 4735.595 |
| | ... | ... | ... | 4676.932 | 4863.014 | 4759.839 |
| | | | 5242.003 | 5369.507 | 5329.227 | |

| | | | |
|--|-----------|-----------|-----------|
| | 5323.938 | 5458.651 | 5371.789 |
| | 5333.295 | 5520.962 | 5422.958 |
| | 5439.980 | 5600.705 | 5490.967 |
| | 5512.622 | 5689.231 | 5557.024 |
| | 5738.918 | 5860.734 | 5790.181 |
| | 5885.420 | 6045.610 | 5939.565 |
| | 5933.952 | 6170.127 | 6047.993 |
| | 6093.551 | 6284.161 | 6177.464 |
| | 23481.562 | 23607.903 | 23550.890 |
| | ... | ... | ... |

Table S10 Comparative g_x , g_y , g_z for 8 lowest Kramers doublets of the Tb1-Tb3 centers of the Tb₃ molecule.

| ID | 1 | | 2 | | 3 | | |
|----|-----------------------|---------|-----------------------|---------|-----------------------|---------|--------|
| | E (cm ⁻¹) | g | E (cm ⁻¹) | g | E (cm ⁻¹) | g | |
| 1 | g_x | 0.000 | | 0.000 | | 0.000 | |
| | g_y | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| | g_z | 0.131 | 16.833 | 0.029 | 17.839 | 0.090 | 17.837 |
| 2 | g_x | | 0.000 | | 0.000 | | 0.000 |
| | g_y | 22.579 | 0.000 | 142.214 | 0.000 | 106.225 | 0.000 |
| | g_z | 26.390 | 14.229 | 144.587 | 14.415 | 107.496 | 14.711 |
| 3 | g_x | | 0.000 | | 0.000 | | 0.000 |
| | g_y | 59.529 | 0.000 | 235.247 | 0.000 | 171.446 | 0.000 |
| | g_z | 80.723 | 10.958 | 242.520 | 10.822 | 178.386 | 11.853 |
| 4 | 100.832 | --- | 292.435 | --- | 214.780 | --- | |
| 5 | g_x | | 0.000 | | 0.000 | | 0.000 |
| | g_y | 148.959 | 0.000 | 330.380 | 0.000 | 235.191 | 0.000 |
| | g_z | 154.370 | 10.675 | 356.951 | 11.827 | 242.988 | 9.904 |
| 6 | g_x | | 0.000 | | 0.000 | | 0.000 |
| | g_y | 275.726 | 0.000 | 390.849 | 0.000 | 275.819 | 0.000 |
| | g_z | 279.138 | 12.771 | 402.843 | 16.196 | 277.512 | 14.113 |
| 7 | g_x | | 0.000 | | 0.000 | | 0.000 |
| | g_y | 347.074 | 0.000 | 623.244 | 0.000 | 485.772 | 0.000 |
| | g_z | 348.359 | 15.384 | 623.458 | 17.720 | 485.818 | 17.685 |

Table S11: g-factors and main magnetic axes (3×3) for 8 lowest Ising doublets of the Tb1 center from Tb₃ complex.

| | | | | | | |
|----------|---------|----------------|--------|---------|---------|---------|
| 1 | 0.000 | g _X | 0.000 | 0.2174 | -0.0449 | 0.9750 |
| | 0.131 | g _Y | 0.000 | -0.5114 | 0.8455 | 0.1530 |
| | | g _Z | 16.833 | -0.8313 | -0.5319 | 0.1608 |
| 2 | 22.579 | g _X | 0.000 | 0.0821 | -0.4489 | -0.8897 |
| | 26.390 | g _Y | 0.000 | -0.8012 | 0.5012 | -0.3268 |
| | | g _Z | 14.229 | -0.5927 | -0.7397 | 0.3184 |
| 3 | 59.529 | g _X | 0.000 | 0.7879 | -0.5836 | -0.1964 |
| | 80.723 | g _Y | 0.000 | 0.2842 | 0.0615 | 0.9567 |
| | | g _Z | 10.958 | -0.5462 | -0.8096 | 0.2144 |
| 4 | 100.832 | | --- | --- | --- | --- |
| 5 | 148.959 | g _X | 0.000 | 0.4098 | 0.9121 | 0.0000 |
| | 154.370 | g _Y | 0.000 | 0.4493 | -0.2019 | -0.8702 |
| | | g _Z | 10.675 | -0.7937 | 0.3566 | -0.4926 |
| 6 | 275.726 | g _X | 0.000 | -0.6947 | -0.5557 | 0.4565 |
| | 279.138 | g _Y | 0.000 | 0.1970 | -0.7576 | -0.6222 |
| | | g _Z | 12.771 | 0.6916 | -0.3423 | 0.6359 |
| 7 | 347.074 | g _X | 0.000 | 0.1530 | -0.3204 | -0.9348 |
| | 348.359 | g _Y | 0.000 | -0.6540 | -0.7419 | 0.1472 |
| | | g _Z | 15.384 | 0.7407 | -0.5889 | 0.3231 |

Table S12: Relative angles between the main anisotropy axes in different doublet states of the Tb1 center from Tb₃ complex.

| | | | | | | |
|----------|-------|-------|-------|-------|-------|-------|
| 1 | 0.00 | 20.36 | 23.17 | 66.99 | 73.10 | 75.49 |
| 2 | 20.36 | 0.00 | 7.67 | 88.12 | 84.34 | 84.93 |
| 3 | 23.17 | 7.67 | 0.00 | 87.75 | 87.96 | 81.87 |
| 5 | 66.99 | 88.12 | 87.75 | 0.00 | 10.12 | 16.81 |
| 6 | 73.10 | 84.34 | 87.96 | 10.12 | 0.00 | 23.15 |
| 7 | 75.49 | 84.93 | 81.87 | 16.81 | 23.15 | 0.00 |

Table S13: *g*-factors and main magnetic axes (3×3) for 8 lowest Ising doublets of the Tb₂ center from Tb₃ complex.

| | | | | | | |
|----------|---------|----------------------|--------|---------|---------|---------|
| | | | | | | |
| 1 | | <i>g_X</i> | 0.000 | -0.6164 | -0.1168 | -0.7787 |
| | 0.000 | <i>g_Y</i> | 0.000 | 0.7502 | -0.3875 | -0.5357 |
| | 0.029 | <i>g_Z</i> | 17.839 | -0.2392 | -0.9144 | 0.3265 |
| 2 | | <i>g_X</i> | 0.000 | 0.8973 | -0.4413 | 0.0000 |
| | 142.214 | <i>g_Y</i> | 0.000 | -0.1495 | -0.3039 | -0.9408 |
| | 144.587 | <i>g_Z</i> | 14.415 | 0.4152 | 0.8442 | -0.3387 |
| 3 | | <i>g_X</i> | 0.000 | 0.3285 | -0.7074 | -0.6257 |
| | 235.247 | <i>g_Y</i> | 0.000 | -0.7529 | 0.2037 | -0.6257 |
| | 242.520 | <i>g_Z</i> | 10.822 | -0.5701 | -0.6767 | 0.4657 |
| 4 | 292.435 | | --- | --- | --- | --- |
| 5 | | <i>g_X</i> | 0.000 | 0.4345 | 0.7028 | -0.5631 |
| | 330.380 | <i>g_Y</i> | 0.000 | -0.4206 | 0.7112 | 0.5631 |
| | 356.951 | <i>g_Z</i> | 11.827 | 0.7963 | -0.0078 | 0.6047 |
| 6 | | <i>g_X</i> | 0.000 | 0.6535 | 0.7568 | 0.0000 |
| | 390.849 | <i>g_Y</i> | 0.000 | -0.5667 | 0.4893 | -0.6628 |
| | 402.843 | <i>g_Z</i> | 16.196 | -0.5016 | 0.4331 | 0.7487 |
| 7 | | <i>g_X</i> | 0.000 | -0.3652 | -0.9237 | 0.1150 |
| | 623.244 | <i>g_Y</i> | 0.000 | 0.5135 | -0.3029 | -0.8028 |
| | 623.458 | <i>g_Z</i> | 17.720 | 0.7764 | -0.2341 | 0.5850 |

Table S14: Relative angles between the main anisotropy axes in different doublet states of the Tb₂ center from Tb₃ complex.

| | | | | | | |
|----------|-------|-------|-------|-------|-------|-------|
| 1 | 0.00 | 10.90 | 24.87 | 89.19 | 88.19 | 77.33 |
| 2 | 10.90 | 0.00 | 15.00 | 78.05 | 79.78 | 74.81 |
| 3 | 24.87 | 15.00 | 0.00 | 80.38 | 70.02 | 89.33 |
| 5 | 89.19 | 78.05 | 80.38 | 0.00 | 87.14 | 13.10 |
| 6 | 88.19 | 79.78 | 70.02 | 87.14 | 0.00 | 86.97 |
| 7 | 77.33 | 74.81 | 89.33 | 13.10 | 86.97 | 0.00 |

Table S15: g-factors and main magnetic axes (3×3) for 8 lowest Kramers doublets of the Tb³⁺ center from Tb₃ complex.

| | | | | | | |
|----------|---------|----------------|--------|---------|---------|---------|
| 1 | 0.000 | g _X | 0.000 | -0.0303 | -0.0830 | -0.9960 |
| | 0.090 | g _Y | 0.000 | 0.9391 | -0.3434 | 0.0000 |
| | | g _Z | 17.837 | 0.3421 | 0.9354 | -0.0884 |
| 2 | 106.225 | g _X | 0.000 | 0.0257 | -0.0364 | -0.9990 |
| | 107.496 | g _Y | 0.000 | -0.8815 | 0.4704 | -0.0398 |
| | | g _Z | 14.711 | -0.4714 | -0.8816 | 0.0199 |
| 3 | 171.446 | g _X | 0.000 | 0.8011 | -0.5985 | 0.0000 |
| | 178.386 | g _Y | 0.000 | 0.0589 | 0.0789 | -0.9951 |
| | | g _Z | 11.853 | 0.5955 | 0.7972 | 0.0984 |
| 4 | 214.780 | | --- | --- | --- | --- |
| 5 | 235.191 | g _X | 0.000 | -0.0505 | -0.9966 | -0.0648 |
| | 242.988 | g _Y | 0.000 | 0.9986 | -0.0495 | -0.0158 |
| | | g _Z | 9.904 | 0.0125 | -0.0655 | 0.9977 |
| 6 | 275.819 | g _X | 0.000 | -0.8362 | 0.5145 | 0.1898 |
| | 277.512 | g _Y | 0.000 | 0.4435 | 0.8380 | -0.3177 |
| | | g _Z | 14.113 | 0.3225 | 0.1814 | 0.9289 |
| 7 | 485.772 | g _X | 0.000 | 0.4999 | 0.8660 | 0.0000 |
| | 485.818 | g _Y | 0.000 | 0.2984 | -0.1723 | -0.9387 |
| | | g _Z | 17.685 | -0.8129 | 0.4693 | -0.3446 |

Table S16: Relative angles between the main anisotropy axes in different doublet states of the Tb³⁺ center from Tb₃ complex.

| | | | | | | |
|----------|-------|-------|-------|-------|-------|-------|
| 1 | 0.00 | 8.94 | 19.81 | 81.65 | 81.86 | 78.97 |
| 2 | 8.94 | 0.00 | 10.98 | 88.84 | 87.54 | 81.27 |
| 3 | 19.81 | 10.98 | 0.00 | 86.93 | 82.01 | 81.72 |
| 5 | 81.65 | 88.84 | 86.93 | 0.00 | 19.46 | 67.36 |
| 6 | 81.86 | 87.54 | 82.01 | 19.46 | 0.00 | 48.12 |
| 7 | 78.97 | 81.27 | 81.72 | 67.36 | 48.12 | 0.00 |